# Urban Computing

Dr. Mitra Baratchi

Leiden Institute of Advanced Computer Science - Leiden University

March 13, 2020



Universiteit Leiden The Netherlands

▲ロト ▲帰 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

Third Session: Urban Computing - Machine learning

# Recap (Session 2-4)

- Time-series data
- Spatial data
  - Geostatistical processes (e.g. temperature)
  - Point processes (e.g. crime)
  - Lattice processes (e.g. population)
- Spatio-temporal data
  - Spatio-temporal processes (extension of spatial processes)
  - Spatio-temporal trajectories
- There is a lot of statistical basis in analysis of spatial, temporal, and spatio-temporal data (autocorrelation, auto-regressive models, kriging, point patterns, processes, etc.)
- This has been followed up by a new trend in machine learning as new data sources (trajectory data) became available

## Agenda for this session

- ▶ Part 1: Machine learning for spatio-temporal data
- Part 2: Modeling spaces
  - Spatial profiling
- Part 3: Modeling individual trajectories
  - Trajectory clustering
  - Trajectory forecasting
- Part 4: Modeling social trajectories
  - Memory-based POI recommendation

Model-based POI recommendation

Part 1: Machine learning for spatio-temporal data

Machine learning for spatio-temporal data

How can we use machine learning algorithms to deal with data of spatio-temporal nature with the following properties?

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

# Machine learning for spatio-temporal data

How can we use machine learning algorithms to deal with data of spatio-temporal nature with the following properties?

- High dimensional (in time and space)
- Auto-correlation in time and space
- Non-stationarity in time, heterogeneity in space
- Multi-scale effect
- Many types of imperfections (noise, missing data, inconsistent sampling rate)

## Machine learning for spatio-temporal data

- Do we know any algorithms that is suited for high-dimensional data?
- Do you know any machine learning algorithm that is inherently aware of space (areas, distances, neighborhoods) and time (periodicity, durations, intervals, etc.)?

Do you know any machine learning algorithm that is inherently robust to noise, missing data, etc.? Challenges in spatio-temporal data analysis

#### Machine learning for spatio-temporal data

General purpose algorithms are not designed for spatio-temporal data. The key is to adapt available algorithms to spatio-temporal data?

#### Not Secure | urban.cs.wpi.edu/urbcomp2019/



#### Aims and Scope

The goals and framework of urban computing result in four folds of challenges in the context of data mining:

- Adapt machine learning algorithms to spatial and spatio-temporal data: Spatio-temporal data has unique properties, consisting of
  spatial distance, spatial hierarchy, temporal smoothness, period and trend, as compared to image and text data. How to adapt existing
  machine learning algorithms to deal with spatio-temporal provinties remains a challenge.
- Combine machine learning algorithms with database techniques: Machine learning and databases are two distinct fields in computing
  science, having their own communities and conferences. While people from these two communities barely talk to each other, we do need the
  knowledge from both sides when designing data analytic methods for urban computing. The combination is also imperative for other big
  data projects. It is a challenging task for people from both communities to design effective and efficient data analytics methods that
  seamlessly and organically integrate the knowledge of databases and machine learning.
- Cross-domain knowledge fusion methods: While fusing knowledge from multiple disparate datasets is imperative in a big data project, cross-domain data fusion is a non-trivial task given the following reasons. First, simply concatenating features extracted from different datasets into a single feature vector may compromise the performance of a task, as different data sources may have very different feature spaces, distributions and levels of significance. Second, the more types of data involved in a task, the more likely we could encounter a data scarce problem. For example, two data sources, consisting of traffic, meteorology, POIs, road networks, and air quality readings, are used to predict the fine-grained air quality throughout a city. When trying to apply this method to other cities, however, we would find that many cities cannot find enough data in each domain (e.g. do not have enough monitoring stations to generate air quality data), or may even not have the data of a domain (its traffic data) all.
- Interactive visual data analytics: Data visualization is not solely about displaying raw data and presenting results, though the two are
  general motivation of using visualization. Interactive visual data analytics becomes even more important in urban computing, seamlessly
  combining visualization methods with data mining algorithms as well as a deployment of the integration on a cloud computing platform. It
  is also an approach to the combination of human intelligence with machine intelligence. The interactive visual data analytics basic empower
  people to integrate domain knowledge (such as urban planning) with data science, enabling domain experts to work with data scientist on

#### 🖈 🌻 🗊 🖊 🛅 👂 🛇

#### Questions we often need to answer

- How to define a new machine learning algorithm for a given spatio-temporal problem?
- These are few options for adapting available algorithms:
  - Changing the input data representation
  - Changing the similarity measure
  - Changing the objective function
    - Supervised learning  $\leftarrow$  designing new auto-regressive models

- $\blacktriangleright \ Unsupervised \ learning \leftarrow a \ very \ popular \ approach$
- Requires thinking about a means for evaluating the performance
- How to find algorithms that are both aware of space and time?
- How to deal with data imperfections algorithmically?

# Data look

	Id 2635 2635 2635 2635 2635 2635	Timestan 1997-07- 1997-07- 1997-07- 1997-07- 1997-08-	np 24 20:50:00 24 21:23:35 27 22:30:23 31 02:52:48 03 01:47:04	Location-long - 149.007 - 148.897 - 148.967 - 149.026 - 149.046	Location 63.809 63.766 63.824 63.803 63.795	-lat
Time						GPS
location						
MobileEntity ID, or anything else	->1	Scannerid	Time	DeviceAdd	ress	-
	3	1324	1435505646	724290cde6a	f4645	
	4	1306	1435492293	6f1cf35f0bae	2726	
	5	1293	1435513780	0c6185a840a	4ee04	
	6	1293	1435513780	1eae/d8tde8	dc50a	
	8	1297	1434550410	6404521500	09469	
	9	1297	1434550412	6e05f4edfdf0	8391	
	10	1297	1434550419	a04138e1aff4	18b03	
	11	1297	1434559015	6ea0d773c85	1ed56	
	12	1297	1434550018	58884273fc4	50e86	<u>WiFi</u>
						scans

How people have changed available machine learning algorithms to deal with this data?

In this session we will see few examples:

- Spatial patterns (New features space + K-mean)
- Trajectory clustering (Modified DBSCAN clustering)
- Trajectory forecasting (Modified Hidden Markov Models)
- POI recommendations (Modified recommendation algorithms)

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

What are different ways we can look at trajectory data?

Query type	Location	EntityID	time	
1	Fixed	Fixed	Variable	
2	Fixed	Variable	Variable	
3	Variable	Fixed	Variable	
4	Variable	Variable	Variable	

Table: Different ways of looking at trajectory data

(ロ)、(型)、(E)、(E)、 E) の(の)

Part 2: Modeling spaces

◆□ ▶ < 圖 ▶ < 圖 ▶ < 圖 ▶ < 圖 • 의 Q @</p>

What are different ways we can look at trajectory data?

Query type	Location	Entity	time	
1	Fixed	Fixed	Variable	
2	Fixed	Variable	Variable	
3	Variable	Fixed	Variable	
4	Variable	Variable	Variable	

Table: Different ways of looking at trajectory data

(ロ)、(型)、(E)、(E)、 E) の(の)

Research directions:

- Spatial patterns
- Point of interest labeling

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Example: Spatial profiles, spatial fingerprints (Spaceprints)

# **Profiling locations**

#### Given:

▶ Data in form of  $\{\langle s_i, e_j, t \rangle | i \in 1...N, j \in 1...N, t \in 1...T\}$ 

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

#### Objective:

- Creating profiles for each space s<sub>i</sub>
- Each space should have a unique profile
- Profiles reflect functions of spaces
  - Restaurant
  - Cafe
  - Classroom

▶ ...

### How does the data look like?

Detections of entities with unique identifiers in a space look like this:



- How do we compare spaces to each other based on this form of data?
- ▶ How to represent data? What are instances and attributes?

# Creating instances and attributes

Option 1:

- Instances: Each day in a space
- Attributes: Hourly densities



Figure: Density-based features

#### What other features are relevant?

If we collect data from different spaces (cafes, classrooms, etc.) how can we use such data to create profiles for them so that we see their similarities and differences?

# What features define a space?

What does the profile of cafes look like?

- To answer this question. Let's think about what people do in cafes?
  - Meeting
  - Take away coffee
  - Work
  - Watching sport matches (a cafes next to a sport center)

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

How can we capture these activities in form of features?

# What features define a space?

What does the profile of cafes look like?

- To answer this question. Let's think about what people do in cafes?
  - Meeting
  - Take away coffee
  - Work
  - Watching sport matches (a cafes next to a sport center)
- How can we capture these activities in form of features? possibly people being present synchronously in different windows over time?
  - Density based features do not represent these behaviors

Where can presences over time happen?



◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへで



▲□▶ ▲圖▶ ▲圖▶ ▲圖▶ 二副 - のへで



▲□▶ ▲圖▶ ▲圖▶ ▲圖▶ 二副 - のへで









Presences can happen within many possible windows



◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?



 Looking at these windows and see count the number of people present in them

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 三臣 - のへで



- Looking at these windows and see count the number of people present in them
- We need to determine how to count within a window



Presence in a window is considered together with a resolution of counting

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 三臣 - のへで





◆□ ▶ ◆□ ▶ ◆ □ ▶ ◆ □ ▶ ● ○ ● ● ● ●
Example: Windows over time



◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 三臣 - のへで

### Example: Windows over time



- ► Many groups are possibly formed → in real world each group may be following a common activity
- If the activity is recurring, it can be part of the profile or fingerprint of the space

## Resolution of windows

- We are not sure about the frequency with which devices are being detected. This is device dependent.
- In reality, the number of entities in the same window can be considered using different resolutions. We can consider all of them because we are not sure about a consistent device frequency.



## Creating instances and attributes

Option 2: Spaceprints feature vector [BHvS17]

- Instances: Each day in a space
- Attributes: The number of devices being present in windows w with variable:
  - Starting time t<sub>start</sub>
  - Duration  $\tau$
  - Sampling resolution  $t_s$



### Feature vector

If we calculate all possible features according to same template, we will have a feature vector



A feature vector (FD=168 hr, FR=24 hr)

Figure: 1

This feature spaces can be match with a similarity measure and used within a clustering algorithm (K-means) to can cluster spaces based on similarities

<sup>1</sup>Image sources: [BHvS17]

## Space profiles



Figure: (Left) Option 2: feature vectors acquired from Spaceprint (right) Option 1: feature vectors acquired from density based counting.<sup>2</sup>

<sup>2</sup>Image sources: [BHvS17]

Part 3: Modeling individual trajectories

What are different ways we can look at trajectory data?

Query type	Location	Entity	time
1	Fixed	Fixed	Variable
2	Fixed	Variable	Variable
3	Variable	Fixed	Variable
4	Variable	Variable	Variable

Table: Different ways of looking at trajectory data

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへで

Research directions

- Trajectory clustering
- Trajectory prediction

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

What clustering algorithms exist? Which ones can be useful?

Very popular in trajectory data mining

- Clustering based on density (local cluster criterion), such as density connected points
- Each cluster has a considerably higher density of points
- Advantage: easier parameter setting compared to algorithms such as K-means:

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

• You do not need to define K.

## DBSCAN

- DBSCAN: Density-based spatial clustering of applications with noise
- Two parameters
  - **Eps** ( $\epsilon$ ): Maximum radius of the neighborhood from a point
  - MinPts: Minimum number of points in an Eps-neighborhood of that point

## DBSCAN: Core, Border and Noise Points



- $N_{\epsilon}(q): \{p | dist(p,q) \leq \epsilon\}$
- Directly density-reachable: A point p is directly density-reachable from a point q wrt. ε, MinPts if
  - *p* belongs to  $N_{\epsilon}(q)$
  - core point condition  $|N_{\epsilon}(q)| >= MinPts$

Let's see how can we apply DBSCAN to trajectory data?

◆□ ▶ < 圖 ▶ < 圖 ▶ < 圖 ▶ < 圖 • 의 Q @</p>

Example 1: clustering trajectories

◆□ ▶ < 圖 ▶ < 圖 ▶ < 圖 ▶ < 圖 • 의 Q @</p>

## Objective

#### Given:

A set of trajectories presented in form of multi-dimensional points *Tr* = *p*<sub>1</sub>, *p*<sub>2</sub>, *p*<sub>3</sub>, ..., *p<sub>n</sub>*.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

- A point  $p_i$  is 2-dimensional entity (x, y).
- Trajectories segmented to day level

#### Objective:

- We look for clusters representing frequent patterns
- Clusters represent the most visited path
  - Road segment

## Trajectory clustering

- DBSCAN for trajectory clustering
- Option 1:
  - Take trajectories as data instances
  - Modify DBSCAN to cluster trajectories

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

## Issues with option 1

- Trajectory partitions: If we consider only complete trajectories, we miss valuable information on common Sub-trajectories.
  - Finding the characteristic point of trajectories
- Similarity measure: How to measure the distance between trajectories

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

Option 2: Traclus: An example of using DBSCAN for trajectory clustering [LHW07]

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

## Challenge



Figure: How to find common sub-trajectories?

- Data instances for DBSCAN should represent sub-trajectory candidates
- Partition trajectories to simple line segments first

## Distance function

Now we need a way to measure the distance between line segments?



◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

#### Distance measure



•  $Dist(L_i, L_j) = w_{\perp} . d_{\perp}(L_i, L_j) + w_{||} . d_{||}(L_i, L_j) + d_{\theta} . (L_i, L_j)$ 

- Perpendicular distance:  $d_{\perp} = \frac{l_{\perp 1}^2 + l_{\perp 2}^2}{l_{\perp 1} + l_{\perp 2}}$
- Parallel distance:  $d_{||} = Min(I_{||1}, I_{||2})$
- Angle distance:  $d_{\theta} = ||L_k||sin(\theta)$

Partition and group framework:

- Partition trajectories
- Cluster line segments using DBSCAN modified based on the new similarity measure

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Example 2: trajectory forecasting

<□ > < @ > < E > < E > E のQ @

## Objective

#### Given:

A set of trajectories presented in form of multidimensional points *Tr* = {*p*<sub>1</sub>, *p*<sub>2</sub>, *p*<sub>3</sub>, ..., *p<sub>n</sub>*}.

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

• A point  $p_i$  is 2-dimensional entity (x, y).

#### Objective:

▶ We want to forecast future points of the trajectory {p<sub>n+1</sub>, p<sub>n+2</sub>,...,} What algorithms do we know that can capture temporal aspects? Which ones can be used for forecasting?

Some algorithms are designed to be **aware of time** (sequential order. These are known as **dynamic machine learning**, or **state-space** algorithms

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

- Dynamic Bayesian Networks
- Hidden Markov Model

### Markovian process

- A Markov process can be thought of as memory-less
  - The future of the process is solely based on its present state just as well as one could know the process's full history.



 $p(x_n|x_1,...,x_{n-1}) = p(x_n|x_{n-1})$ 

## Hidden Markov model



A Hidden Markov Model is defined by finding the following parameters:

- X States
- Y Observations
- A State transition probabilities
  - *a<sub>ij</sub>* is probability of transition from state *i* to *j*
- B output probabilities
  - b<sub>ij</sub> is probability emission state i to observation j

π Initial state

## Hidden Markov Model

- ▶ Option 1: using Hidden Markov Model to model trajectories → instances are points on trajectories
- Issue with Option 1:
  - Trajectories are composed of movements with high speed and almost zero speed
  - Staying at home for 5 hours, being at work for 8 hours, ...
  - ► States are meaningful if the durations is considered → Hidden semi Markov model considers an extra duration distribution for states

## Hidden semi Markov Model (HSMM)

Give instances as ordered trajectory points in time the following model parameters should be calculated:

- A (transitions matrix)
- B (emission matrix)
- Π (initial state vector)
- ► D (State duration distribution) ← New parameter in the HSMM

How estimated these parameters?

Different algorithms exist that can be used to extract these model parameters from the data:

- Baum welch
- Viterbi,
- etc

# Hierarchical HSMM on human mobility data [BMH<sup>+</sup>14]

We will be able to find:

- Super states with duration of weekdays and week ends
- > States with the duration of hours of stay in different locations



<sup>3</sup>image source: [BMH<sup>+</sup>14]

## Example of Hierarchical HSMM on Geolife data



<sup>4</sup>image source: [BMH<sup>+</sup>14]

▲ロト ▲園ト ▲ヨト ▲ヨト ニヨー のへ(で)

Part 3: Modeling social trajectories

### What are different ways we can look at trajectory data

Query type	Location	Entity	time
1	Fixed	Fixed	Variable
2	Fixed	Variable	Variable
3	Variable	Fixed	Variable
4	Variable	Variable	Variable

Table: Different ways of looking at trajectory data

(ロ)、(型)、(E)、(E)、 E) の(の)

Research directions:

Understanding users' interests based upon their locations.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

Understanding locations' functions via user mobility.

### Point of interest (POI) recommendation
### POI recommendation

#### Given:

 ▶ Given data U = {u<sub>1</sub>, u<sub>2</sub>, ...u<sub>n</sub>} a set of users, and L = {l<sub>1</sub>, l<sub>2</sub>, ...l<sub>m</sub>} a set of POIs, and C = {c<sub>1,1</sub>, ..., c<sub>i,j</sub>} a set of check-ins of users in POIs where c<sub>i,j</sub> denotes the number of times user u<sub>i</sub> checked in l<sub>j</sub>

#### Objective:

- Recommending a location to a user through inferring the preference of the user to check-in to a location they have not checked-in before
- Predicting if this user will ever check-in to a POI (time is not that important)
- Performance is typically measured through precision and recall of top K recommended locations

## **POI** recommendation

- Recommender systems are information filtering systems which attempt to predict the rating or preference that a user would give, based on ratings that similar users gave and ratings that the user gave on previous occasions.
- Many different types of Location-Based Social Networks (LBSN) (Foursquare, Brightkite, Gowalla)
- These are the context information we want the recommender system for LBSN to be aware of

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

# Challenges pf POI recommendation

- Implicit feedback: check-ins, visits rather than explicit feedback in form of ratings
- ▶ Data sparsity: A lot of places do not have visit data, For example, the sparsity of Netflix data set is around 99%, while the sparsity of Gowalla is about 2.08 × 10<sup>-4</sup>%

- Cold start:
  - New locations have no ratings
  - New users have no history
- **Context**: we want the algorithms to be aware of:
  - Spatial influence
  - Social influence
  - Temporal influence

What recommendation algorithms exist? Which ones can be useful?

# Collaborative filtering

- Memory-based
  - User-based
  - Item-based
- Model-based
  - Matrix factorization

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

SVD

Example 1: Memory-based POI recommendation

◆□ ▶ < 圖 ▶ < 圖 ▶ < 圖 ▶ < 圖 • 의 Q @</p>

#### Memory-based

- Memory-based: Uses memory of past ratings
- K-nearest neighbor: Using data of nearest neighbors
- Predicting ratings by getting an average of ratings:
  - User-based: ratings based on a user's most similar neighbors
  - Item-based: ratings of a user based on an item's most similar neighbors

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

We need to measure the similarity between users based on their check-in history

► The first component of user-based POI recommendation algorithm is determining how to compute the similarity weight sim(u, v) between user u and v.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

# Collaborative filtering, similarity

	item <sub>1</sub>	item <sub>2</sub>	item <sub>3</sub>	item <sub>4</sub>	item <sub>5</sub>	item <sub>6</sub>	item <sub>3</sub>
$u_1$	4			5	1		
<i>u</i> <sub>2</sub>	5	5	4				
u <sub>3</sub>				2	4	5	
<i>u</i> 4		3					3

- Consider  $u_i$  and  $u_j$  with rating vectors  $r_i$  and  $r_j$
- ► Intuitively capture this: sim(u<sub>1</sub>, u<sub>2</sub>) > sim(u<sub>1</sub>, u<sub>3</sub>)

# Cosine similarity

	item <sub>1</sub>	item <sub>2</sub>	item <sub>3</sub>	item <sub>4</sub>	item <sub>5</sub>	item <sub>6</sub>	item <sub>3</sub>
$u_1$	4			5	1		
<i>u</i> <sub>2</sub>	5	5	4				
u <sub>3</sub>				2	4	5	
U4		3					3
		r <sub>i</sub> .r <sub>i</sub>		r <sub>i</sub> .r <sub>i</sub>			

<□ > < @ > < E > < E > E のQ @

• 
$$sim(u_i, u_j) = \frac{u_i u_j}{||r_i|| ||r_j||} = \frac{u_i u_j}{\sqrt{\sum_i r_i^2} \sqrt{\sum_i r_j^2}}$$

# Cosine similarity

	item <sub>1</sub>	item <sub>2</sub>	item <sub>3</sub>	item <sub>4</sub>	item <sub>5</sub>	item <sub>6</sub>	item <sub>3</sub>		
$u_1$	4			5	1				
<i>u</i> <sub>2</sub>	5	5	4						
U3				2	4	5			
U4		3					3		
• $sim(u_i, u_j) = \frac{r_i \cdot r_j}{  r_i   \   r_j  } = \frac{r_i \cdot r_j}{\sqrt{\sum_i r_i^2} \sqrt{\sum_i r_j^2}}$									

replace empty with 0

## Cosine similarity

	item <sub>1</sub>	item <sub>2</sub>	item <sub>3</sub>	item <sub>4</sub>	item <sub>5</sub>	item <sub>6</sub>	item3
$u_1$	4			5	1		
<i>u</i> <sub>2</sub>	5	5	4				
U <sub>3</sub>				2	4	5	
<i>u</i> 4		3					3

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

• 
$$sim(u_i, u_j) = \frac{r_i \cdot r_j}{||r_i|| \ ||r_j||} = \frac{r_i \cdot r_j}{\sqrt{\sum_i r_i^2} \sqrt{\sum_i r_j^2}}$$

- replace empty with 0
- $sim(u_1, u_2) = 0.38, sim(u_1, u_3) = 0.32$

# Cosine similarity for check-ins

If we replace the **rating vector** by the user's **check-in vector** we can measure similarities.

- Check-ins are often very sparse, we can consider binary check-in vectors
- $c_{ij} = 1$  if user  $u_i$  has checked in  $l_j \in L$  before
- The cosine similarity weight between users  $u_i$  and  $u_k$ ,

• 
$$w_{ik} = \frac{\sum_{l_j \in L} c_{ij} c_{kj}}{\sqrt{\sum_{l_j \in L} c_{ij}^2} \sqrt{\sum_{l_j \in L} c_{kj}^2}}$$

Recommendation score based on k most similar users

$$\hat{c}_{ij} = \frac{\sum_{u_k} w_{ik} c_k}{\sum_{u_k} w_{ik}}$$

# Context: Geographic influence

- How to include geographical influences?
- The Toblers First Law of Geography is also represented as geographical clustering phenomenon in users check-in activities.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

## Context: Geographic influence

- How to include geographical influences?
- The Toblers First Law of Geography is also represented as geographical clustering phenomenon in users check-in activities.
  - Activity area of users: Users prefer to visit nearby POIs rather than distant ones; people tend to visit POIs close to their homes or offices
  - Influence area of POIs: People may be interested in visiting POIs close to the POI they are in favor of even if it is far away from their home; users may be interested in POIs surrounded a POI that users prefer.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

Different ways for considering the geographic influences [YC15]

▲ロト ▲帰 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

- Power-law based model
- Distance based model
- Multi-center Gaussian model

# Power-law geographical model [YYLL11]

- Check-in probability follows power law distribution
- $y = a \times x^b$ 
  - x and y refer to the distance between two POIs visited by the same user and its check-in probability
  - *a* and *b* are parameters of power law distribution
- ► For a given POI *lj*, user *u<sub>i</sub>*, and her visited POI set *L<sub>i</sub>*, the probability of *u<sub>i</sub>* to check in *l<sub>j</sub>* is:

$$\blacktriangleright P(l_j|L_i) = \frac{P(l_j \cup L_i)}{P(L_i)} = \prod_{l_y \in L_i} P(d(l_j, l_y))$$



Figure: Check-in probabilities may follow a power law distribution <sup>5</sup>

・ロト ・四ト ・ヨト ・ヨト ・ヨ

<sup>&</sup>lt;sup>5</sup>Image source [YYLL11]

# Multi-center geographical influence

Geographical influence, multi-center

- Check-ins happen near a number of centers
  - Work area
  - Home area
  - etc.



# Multi-center geographical influence

- Probability of check-in of user u in location I
- Probability of I belonging to any of those centers

• 
$$P(I|C_u) = \sum_{c_u=1}^{|C_u|} P(I \in c_u) \frac{f_{c_u}^{\alpha}}{\sum_{i \in C_u} f_i^{\alpha}} \frac{N(I|\mu c_u), \sum_{C_u}}{\sum_{i \in C_u} N(I|\mu_i, \sum_i)}$$

- ▶ Where  $P(l \in c_u) = \frac{1}{d(l,c_u)}$  is the probability of POI *l* belonging to the center  $c_u$ ,
- $\frac{f_{c_u}^{\alpha}}{\sum_{i \in C_u} f_i^{\alpha}}$  is the normalized effect of check-in frequency on the center  $c_u$  and parameter  $\alpha$  maintains the frequency aversion property

► N(I|µC<sub>u</sub>) is the probability density function of Gaussian distribution

# Social influence

- Depending on a source, social information may also be available which can be used to improve the recommendation performance
- The social influence weight between two friends u<sub>i</sub> and u<sub>k</sub> based on both of their social connections and similarity of their check-in activities

$$\blacktriangleright SI_{kj} = \nu \cdot \frac{|F_k \cap F_i|}{|F_k \cup F_i|} + (1 - \nu) \frac{|L_k \cap L_i|}{|L_k \cup L_i|}$$

- $\nu$  is a tuning parameter ranging within [0, 1]
- $F_k$  and  $L_k$  denote the friend set and POI set of user  $u_k$

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

How to put all information in one model?

A recommender system which has embedded all these influences?

(ロ)、(型)、(E)、(E)、 E) の(の)

### How to put all information in one model?

- A recommender system which has embedded all these influences?
  - Fused model: The fused model fuses recommended results from collaborative filtering method and recommended results from models capturing geographical influence, social influence, and temporal influence.

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > <

#### Fused model

- Check-in probability of user i in location j:
- $\triangleright S_{i,j} = (1 \alpha \beta)S_{i,j}^{u} + \alpha S_{i,j}^{s} + \beta S_{i,j}^{g}$ 
  - ► S<sup>u</sup><sub>i,j</sub>, S<sup>s</sup><sub>i,j</sub>, S<sup>g</sup><sub>i,j</sub> are user preference, social influence, and geographical influence
  - where (α and β) (0 ≤ α + β ≤ 1) are relative importance of social influence and geographical influence

Example 2: Model-based POI recommendation

◆□ ▶ < 圖 ▶ < 圖 ▶ < 圖 ▶ < 圖 • 의 Q @</p>

## Model-based recommendation

- Latent variable models: how to model users and POIs without having any features of them? (e.g. is there a latent factor showing how cosy a place is?)
- Build the hidden model of a user: what does a user look for in a POI?
- Build the hidden model of an item: what does a POI offer to users?

- Methods:
  - Matrix factorization
  - Singular value decomposition

## Factorization: Latent factor models

Assume that we can approximate the rating matrix R as a product of U and  $P^T$ 

▲ロト ▲帰 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()



How do we find U and P matrices?

Singular value decomposition SVD

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

▶ ....

# SVD (Singular value decomposition)



- Σ is a diagonal where entries are positive and sorted in decreasing order
- U and V are column orthogonal:  $U^T U = I$ ,  $V^T V = I$
- This leads to a unique decomposition  $U, V, \Sigma$

# Optimizing by solving this problem

- Find matrices U and  $\Sigma$  and V that minimize this expression
- $\min_{U,V,\Sigma} \sum_{i,j \in A} (A_{ij} [U\Sigma V^T]_{ij})^2$
- In case of sparse matrices we have to makes sure that error is calculated on the non-zero elements

How to include other context in a matrix factorization model?

Joint model: The joint model establishes a joint model to learn the user preference and the influential factors together

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Two different types of joint models:

- Incorporating factors (e.g., geographical influence and temporal influence) into traditional collaborative filtering model like matrix factorization and tensor factorization
- Generating a graphical model according to the check-ins and extra influences like geographical information.

Joint geographical modeling and matrix factorization

Augment user's and POI's latent factors with geographical influence

- Activity areas of a user are determined by the grid area where the user may show up and a number indicating the possibility of appearing in that area
- Influence area of a POI are the grid cells to which the influence of this POI can be propagated and a number quantifying the influence from this POI.

# Joint geographical modeling and matrix factorization [LZX<sup>+</sup>14]



Figure: Geo matrix factorization

イロト 不得下 不良下 不良下 一度

• **MF**:  $R = UP^T$ 

- **GeoMF**:  $R = UP^T + XY^T$ 
  - X is users' activity area matrix
  - Y is POIs' influence area matrix

# Generating influence areas

The influence areas can be captured in the following manner and be added to the GeoMF model



6

## Lessons learned

- There is a considerable body of work in urban computing trying to adapt available ML algorithms to spatio-temporal data
- When dealing with a new ML problem for spatio-temporal data:
  - First identify the temporal and spatial factors you want to consider
  - Ask yourselves what ML algorithms have the potential to solve this problem?
    - Spatial clustering offered by DBSCAN
    - Temporal modeling offered by dynamic models
    - Joint user-POI modeling offered by information filtering algorithms
  - Identify how you can adapt the selected algorithm by augmenting it with other spatial and temporal modeling capabilities
  - See if you can find a good way to deal with noise, missing data, inconsistent sampling issues of data algorithmically.

#### References I

- Mitra Baratchi, Geert Heijenk, and Maarten van Steen, Spaceprint: A mobility-based fingerprinting scheme for spaces, Proceedings of the 25th ACM SIGSPATIAL International Conference on Advances in Geographic Information Systems (New York, NY, USA), SIGSPATIAL '17, ACM, 2017, pp. 102:1–102:4.
- Mitra Baratchi, Nirvana Meratnia, Paul JM Havinga, Andrew K Skidmore, and Bert AKG Toxopeus, A hierarchical hidden semi-markov model for modeling mobility data, Proceedings of the 2014 ACM International Joint Conference on Pervasive and Ubiquitous Computing, ACM, 2014, pp. 401–412.
## References II

- Jae-Gil Lee, Jiawei Han, and Kyu-Young Whang, *Trajectory clustering: a partition-and-group framework*, Proceedings of the 2007 ACM SIGMOD international conference on Management of data, ACM, 2007, pp. 593–604.
- Defu Lian, Cong Zhao, Xing Xie, Guangzhong Sun, Enhong Chen, and Yong Rui, Geomf: joint geographical modeling and matrix factorization for point-of-interest recommendation, Proceedings of the 20th ACM SIGKDD international conference on Knowledge discovery and data mining, ACM, 2014, pp. 831–840.
- Andrey Tietbohl Palma, Vania Bogorny, Bart Kuijpers, and Luis Otavio Alvares, *A clustering-based approach for discovering interesting places in trajectories*, Proceedings of the 2008 ACM symposium on Applied computing, ACM, 2008, pp. 863–868.

## References III

- Yonghong Yu and Xingguo Chen, A survey of point-of-interest recommendation in location-based social networks, Workshops at the Twenty-Ninth AAAI Conference on Artificial Intelligence, 2015.
- Mao Ye, Peifeng Yin, Wang-Chien Lee, and Dik-Lun Lee, Exploiting geographical influence for collaborative point-of-interest recommendation, Proceedings of the 34th international ACM SIGIR conference on Research and development in Information Retrieval, ACM, 2011, pp. 325–334.